

# **FRICITION ON CRACK SURFACES DURING COMPRESSION OF EXPLOSIVES – A POSSIBLE IGNITION SOURCE FOR UNPLANNED EXPLOSIONS DUE TO ACCIDENTAL DEFORMATIONS**

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## **ABSTRACT**

The mechanical properties of composite plastic bonded explosives have been investigated as a function of confining pressure. The results indicate different failure processes in two pressure ranges, a low pressure range between about 0.1 to 7.0 MPa which is considered in this paper and a higher pressure range. In the low pressure range crack processes are important in failure. The pressure dependence of the compressive strength in the low pressure range is attributed to coulomb friction between surfaces of closed shear cracks and from the observed linear increase of the strength with pressure and the angle of the fracture plane a friction coefficient is obtained. A friction coefficient can also be obtained from the ratio of the compressive to tensile strength and directly from the above angle. The friction coefficients obtained from these three separate observations are in agreement and this is taken as strong evidence for the importance of this friction in determining strength and mechanical failure. Frictional heating during deformation can then cause hot spots leading to ignition.

## **1. INTRODUCTION**

Explosives and propellants are often used under conditions of confinement and pressurization. Explosives are confined in projectile cases and are pressurized during launch by set back forces and during impact by set forward forces. Propellants are confined by the breech and are pressurized by hot gases during burning. Because of these pressurizations the properties of explosives and propellants under pressure are of interest. In particular the mechanical properties under pressure are needed for modeling and safety considerations. For example, for the modeling of an explosive filled projectile during launch or impact the mechanical properties of the explosive under pressure are required. Similarly, for the modeling of a propellant charge during burning the mechanical properties of the propellant under pressure are required. Of particular concern are the mechanical failure properties under pressure. Fracture or yield during the use of explosives can lead to unwanted and/or hazardous ignitions (Howe et al, 1985) (Frey, 1985) (Coffee, 1985) (Heavens and

Fields, 1972). In addition, the fracture of propellants during burning can lead to hazardous burning conditions (Nicolaidis et al, 2000). The results presented here also indicate the possible hazards associated with crack processes (Wiegand et al, 2008). Because of these considerations a program has been initiated to study the mechanical properties of these materials under hydrostatic pressure (Wiegand, 2000a, 2000b) (Wiegand and Reddingius, 2003, 2005a, 2005b).

## **2. EXPERIMENTAL**

A high pressure chamber designed at Structural Behavior Engineering Laboratory, Phoenix, AR to contain pressures up to 138 MPa was used to study the compressive mechanical properties as a function of confining pressure (Wiegand, 2000a). Hydraulic oil was used as the confining medium and the sample in the form of a right circular cylinder was protected from the oil by a tight fitting tubular gum rubber or neoprene shroud. The ends of the sample were against steel platens and O-ring seals were used to prevent oil from reaching the sample. (Wiegand, 2000a, 2000b) (Wiegand and Reddingius, 2003, 2005) The confining pressure is taken here as the chamber hydrostatic pressure before the start of and/or during the axial compression. In all cases the pressures referred to here are this hydrostatic pressure. The chamber pressure was determined using a SENSOTEC pressure gauge, model JTE/1108-03, calibrated by the manufacturer and mounted at the base of the chamber. In addition, A McDaniel Controls dial pressure gauge was mounted at the pump. Measurements at atmospheric pressure (0.1 MPa) were made in air.

The samples were compressed along the cylindrical axis and two LVDT's (linear voltage differential transformers) were mounted to measure axial strains. They were spaced 180 degrees apart around the circumference of the sample with their axes parallel to the sample axis. The sample axial strain was taken as the average of the strains obtained from the two LVDT's.. Two or three additional LVDT's were mounted to measure radial strains. They were placed in a plane at the sample axial mid position with their axes perpendicular to the sample axis. They were also 180 degrees apart (or 120

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**TABLE 1**  
**Composition of Composites Discussed**

Name	Explosive/Inert	Binder		T <sub>G</sub> (°C)
		Polymer	Plastizer	
EDC37	HMX	NC	DNEB/TNEB	-63
	91%	1.0%	5.22%/2.78%	
PAX2A	HMX	CAB	BDNPA/F	-37
	85%	6%	9%	
PBS 9501	SUCROSE	ESTANE	BDNPA/F	-41(B) <sup>a</sup>
	94%	3%	3%	
PBX 9501	HMX	ESTANE	BDNPA/F	-41(B) <sup>a</sup>
	95%	2.5%	2.5%	
LX-14	HMX	ESTANE		-31(B) <sup>a</sup>
	95.5%	4.5%		

Nomenclature: HMX - Cyclotetramethylene tetranitramine.. NC - Nitrocellulose. DNEB – Dinitroethylbenzene, TNEB – Trinitroethylbenzene. CAB - Cellulose Acetate Butyrate. BDNPA/F -Bis(2,2-Dinitropropyl)Acetal/Formal. Estane - Polyurethane. B – Property of the Binder.

a (Wiegand and Reddingius, 2005)

degrees for three radial LVDT's) around the sample circumference (Wiegand, 2000a, 2000b) (Wiegand and Reddingius,2003, 2005).

Axial stress versus axial strain data in compression were obtained using the above chamber and an MTS servo-hydraulic system operated at a constant displacement rate (Wiegand, et al, 1991) (Pinto et al, 1985). All work presented was carried out at strain rates of approximately 0.0005/sec. and 0.001/sec with the exception of results explicitly a function of strain rate. The right circular cylinder samples were 3.81 cm (1.50 inch) in length and 1.90 cm (0.75 inch) in diameter and so had a length to diameter ratio of two. The end faces of all samples were coated with a lubricant to minimize frictional effects between the sample end faces and the loading platens. The sample temperatures during measurements were between 20 and 23 C and samples were conditioned at temperature for at least two hours before measurement. The dimensions of all samples at

0.1 MPa (atmospheric pressure) were used to obtain engineering stress and engineering strain.

Most of the measurements reported here were made with samples of EDC37, a UK plastic bonded explosive (PBX). The composition of this explosive is given is Table 1 along with the compositions of other similar materials which are referred to in this paper (Wiegand and Reddingius). Samples were prepared by pressing into large billets and machining to size. Precautions were taken to insure that the cylinder end faces were adequately flat and parallel (Wiegand, 1998).]. The densities of all samples were in a narrow range close to the maximum theoretical (zero porosity) density. The densities of most samples were determined before and after compression by weighing in air and in purified water and by using the density of water at the temperature of measurement. All sensors were calibrated by the manufacturer or calibrated against standards provided by the manufacturer. It is estimated that variations from sample to sample in any measured quantity are significantly greater than errors

introduced by the sensors or errors introduced during data processing.

### 3. RESULTS

The results indicate two pressure ranges in which the mechanical failure properties differ, a low pressure range between about 0.1 and 7.0 MPa for EDC37 in which failure occurs via crack processes and a higher pressure range between about 7.0 and 138 MPa for the same composite, in which failure occurs via slip processes. The low pressure range is here considered in some detail. The higher pressure range is considered elsewhere. (Wiegand, et al, to be published).

In Figure 1 axial stress versus axial strain curves for EDC37 are given for several confining pressures in the low pressure range. The pressures are as marked. The curve at atmospheric pressure (0.1 MPa) has the typical response of many energetic materials at this pressure, and temperature. i.e., an initial linear increase of stress, a maximum stress followed by work softening (decrease of stress) with increasing strain (Wiegand, 1985, 1998). Available evidence indicates that the deviation from linearity after the initial linear region, the maximum and the work softening are associated with crack damage (Wiegand, 1985, 1998). In fact acoustic emission results suggest that some crack damage is generated throughout the stress-strain curve (Ellis et al, 2005). Evidence of surface cracking is observed for most samples deformed into the higher strain parts of the work softening region at atmospheric pressure.

Both the initial slope and the maximum stress increase with increasing pressure while the negative work softening slope decreases with increasing pressure and is close to zero at a pressure of 6.9 MPa. The latter

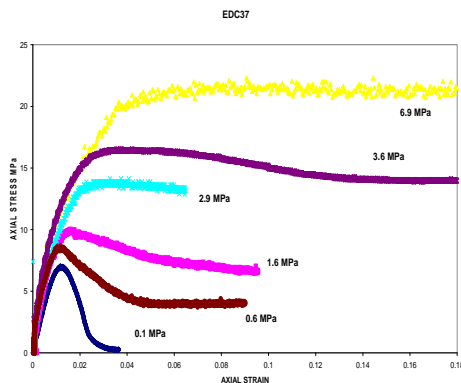


Figure 1. Axial stress versus axial strain for pressures in the low pressure range.

result suggests that either crack damage decreases with increasing pressure and is negligible at 6.9 MPa or that crack damage is generated but that other factors prevent the work softening from being observed. The latter is apparently the case as discussed elsewhere. (Wiegand et al, unpublished) Some what similar results have been obtained for PBS 9501 (Wiegand and Reddingius, 2005a).

In the higher pressure range which is about 7.0 MPa to 138 MPa for EDC37 the slope at larger strains is positive, i.e. work hardening is observed and a maximum in the stress-strain curve is not observed (not shown). In this pressure range the initial slope, which gives the the modulus, the yield strength and the work hardening slope all increased with increasing pressure but are much less sensitive to pressure than the modulus, the compressive strength and the work softening slope in the low pressure range. Somewhat similar results have been obtained for PBS9501 (Wiegand and Reddingius, 2005)) and LX-14 (Wiegand and Reddingius, unpublished results). As noted above the higher pressure range will be discussed in detail elsewhere (Wiegand et al, to be published).

In Figure 2 the compressive strength, the maximum compressive stress, is given versus confining pressure in the low pressure range for EDC37, and a straight line has been fitted to the data points. The results indicate a linear increase with increasing pressure with a slope close to two. Similar results were obtained at other

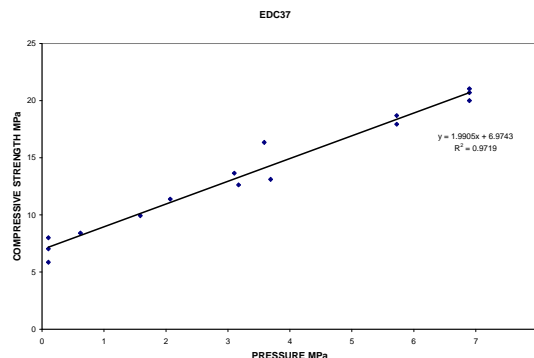


Figure 2. Compressive strength versus pressure for pressures in the low pressure range.

strain rates. More limited results for PBS 9501 also indicate a similar increase of the compressive strength with increasing pressure (Wiegand and Reddingius, 2005). The results of Figures 1 and 2 indicate that crack processes are inhibited by confining pressure, i.e., the stress required at any strain to cause crack damage increases with increasing confining pressure.

As noted above the yield strength for EDC37 also increases with increasing pressure in the higher pressure range (not shown) . However, the slope in the higher pressure range is about 1/40 of the slope of the

compressive strength versus pressure as given in Figure 2 for the low pressure range.

After compression the samples are barreled, i.e., the diameter at the sample mid plane is greater than the diameters at the sample ends. However, in all cases there is an increase in the sample average diameter and a decrease in the average sample length due to deformation.

The dimensions and densities of all samples were measured at atmospheric pressure before and after compression. The dimensions were determined by measurements at several locations on the sample and averaging. As noted above the lengths of all samples after compression are decreased relative to values before compression so that all have permanent negative (compressive) axial strains. In addition, the average diameters of all samples after compression are increased relative to values before compression so that all have positive permanent radial strains. The volumes and densities of most samples were determined by weighing in air and in purified water and by use of the water density at the temperature of measurement. The volumes before and after compression indicate small volume expansions due to deformation. In addition the density measurements indicate small fractional density decreases with deformation ranging from hundredths of a percent up to about 3.9%.

#### 4. DISCUSSION

The results in the low pressure range can be understood on the basis of a friction model developed by Dienes (1983) and Kuo and Dienes (2002). Other authors have also considered the effect of friction on the mechanical properties of materials (McClintock and Walsh, 1962) (Mavko, 1979) (Comninou and Dundurs, 1980) (Tian-Hu and Weishen, 1993) (Egami and Kitaoka, 1996) (Kovtunen, 1998). Dienes (1983) and Zuo and Dienes (2002) have applied the concept of coulomb friction forces between closed shear crack surfaces as resisting crack motion (Ward and Hadley, 1993). This is illustrated by the sketch of Figure 3.  $\sigma_a$  is the applied compressive stress,  $\sigma_{ap}$  is the applied stress on a shear plane,  $p$ , whose normal makes an angle  $\phi$  with the applied stress direction, and  $\sigma_{ps}$  and  $\sigma_{pn}$  are the components of  $\sigma_{ap}$  parallel and perpendicular to the shear plane respectively. These latter stresses are given in terms of  $\sigma_a$  and  $\phi$  as

$$\sigma_{ps} = \sigma_a \cos \phi \sin \phi \quad (1)$$

$$\sigma_{pn} = \sigma_a \cos^2 \phi \quad (2).$$

The net shearing stress on the plane  $p$  is then

$$\sigma_{snet} = \sigma_{ps} - \mu \sigma_{pn} \quad (3)$$

where  $\mu$  is the friction coefficient. And if a hydrostatic pressure  $P$  is applied to the sample in addition to the applied uniaxial stress  $\sigma_a$ , equation (3) becomes

$$\sigma_{snet} = \sigma_{ps} - \mu(\sigma_{pn} + P) \quad (4a)$$

$$= \sigma_a \cos \phi \sin \phi - \mu (\sigma_a \cos^2 \phi + P) \quad (4b)$$

by using equations (1) and (2).

Then equation (4b) can be rearranged to give

$$\sigma_a = (\sigma_{snet} + \mu P) / (\sin \phi \cos \phi - \mu \cos^2 \phi) \quad (5)$$

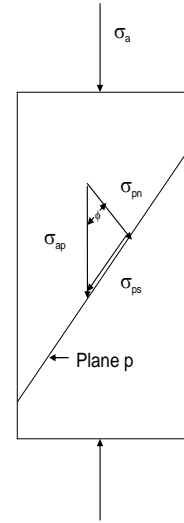


Figure 3. Schematic of stresses for the friction model.

If equation (5) is applied to the maximum of the stress-strain curve, then  $\sigma_{snet}$  is the shear stress at the maximum. Thus  $\sigma_a$  increases linearly with  $P$  as observed (Figure 2) if  $\sigma_{snet}$  is independent of pressure or is linearly dependent on pressure. For the case of  $\sigma_{snet}$  independent of pressure  $\sigma_a$  increases linearly with pressure with a slope of

$$\text{slope} = \mu / (\sin \phi \cos \phi - \mu \cos^2 \phi) \quad (6)$$

The angle  $\phi$  is determined by the plane on which the shear stress,  $\sigma_{\text{net}}$ , is a maximum. By differentiating equation (4b) with respect to  $\phi$  with constant  $\sigma_a$ ,  $\mu$  and  $P$  and setting the differential equal to zero the following is obtained:

$$\tan^2 \phi - 2 \mu \tan \phi - 1 = 0 \quad (7).$$

And by taking the positive route

$$\tan \phi = \mu + (\mu^2 + 1)^{1/2} \quad (8).$$

Thus, by measuring the angle  $\phi$ ,  $\mu$  can be determined from equation (8).  $\mu$  can also be determined from equation (6) using the slope of Figure 2 and the measured value of  $\phi$ . Note that the angle  $\phi$  is independent of  $P$ . It is assumed here that the samples are isotropic and thus that all crack orientations exist.

The angle  $\phi$  can be obtained as the angle that the normal to the fracture surface makes with the applied stress,  $\sigma_a$ , direction (see Figure 3). However, in many cases fracture was not observed but white lines on the sample surfaces were observed in most cases when fracture did not occur. (Fracture was only observed at atmospheric pressure but the white lines were observed at atmospheric pressure and at some elevated pressures in the low pressure range.) These white lines are taken as the precursors of the fracture surfaces and they make approximately the same angle with the applied stress direction as the actual fracture surfaces. Therefore, the angle  $\phi$  has been obtained from the angle of the fracture surface in those cases where fracture was observed and from the angle of the white lines in cases where they were observed. The average value is  $\phi = 61.8$  degrees. By comparison this angle is 45 degrees when  $\mu = 0$  (equation (8)). For plastic bonded explosives this angle has been observed to be greater than 45 degree in most if not all cases, thus indicating the general importance of friction.  $\mu$  as obtained from equation (6) is 0.58, and as obtained from equation (8) is 0.66 and these are listed in Table 2. The agreement of these two values of  $\mu$  supports the assumptions made in obtaining (6).  $\mu$  obtained from equation (6) is expected to be the dynamic coefficient of friction and the value obtained from equation (8) is most probably also the dynamic coefficient.

Dienes (1983) and Kuo and Dienes (2002) also give a relationship between the friction coefficient,  $\mu$ , Poissons' ratio,  $\nu$  and the ratio of compressive to tensile strength as

$$\text{Compressive Strength}_i / \text{Tensile Strength}_i =$$

$$[2(2-\nu)]^{1/2} [(\mu^2+1)^{1/2} + \mu] \quad (9)$$

TABLE 2

Values of the Friction Coefficient,  $\mu$ , Obtained by Using Various Methods

$\mu$	Method of Determining $\mu$
0.58	Slope of Compressive Strength vs. Pressure Curve and the Angle which the Failure Plane Normal makes with the Direction of the Applied Stress - Equation (6)
0.66	The Angle which the Failure Plane Normal makes with the Direction of Applied Stress - Equation (8)
>0.62	The Ratio of Compressive Strength to Tensile Strength - Equation (10)

In equation (9) the compressive strength and the tensile strength are the threshold stresses required to initiate rapid unstable crack growth in compression and tension respectively (Dienes, 1983) (Rice, 1984) (Dienes, 1984). In tension the stress increases in an approximately linear manner with increasing strain to a maximum and then the sample fails in a brittle fashion by fracture (not shown) (Ellis, et al, 2005) (Wiegand, unpublished results). In addition there is very little acoustic emission with increasing tensile stress until the maximum stress is reached (Ellis et al, 2005). This acoustic emission is interpreted as due to elastic waves generated primarily or at least in part by crack processes (Ellis et al, 2005). Thus, the results suggest that there is minimal crack activity until the maximum tensile stress is achieved and that this maximum stress is the stress necessary to initiate rapid unstable crack growth. In contrast, in compression acoustic emission has been observed throughout the increasing stress part of the stress strain curve, through the maximum and into the work softening part of the curve (Ellis et al 2005), but fracture indicating unstable rapid crack growth has not been observed (See the stress-strain curve at atmospheric pressure in Figure 1). It is suggested that only slow crack growth (Charles, 1958) occurs during the compressive stress-strain curve and that the observed acoustic emission is primarily or at least in part due to this slow crack growth. It is further suggested that the damage introduced by this slow crack growth so weakens the sample that the stress required for unstable rapid crack growth in compression is not attained. In some plastic bonded explosives, e.g., PAX 2A rapid unstable crack growth is observed in compression at low temperature (Wiegand, 1999.) However, at 25 C the tensile and compressive stress-strain curves for PAX 2A are very

similar to those of EDC37. Slow crack growth is not expected at low temperatures.

Slow crack growth is thermally activated and stress assisted (Charles, 1958) and does not have an explicit threshold stress. In contrast rapid unstable crack growth does have a threshold stress. Dienes (1998) and Dienes and Reilly (1998) used crack growth models without thresholds to obtain fits to Wiegand's (unpublished results) uniaxial compressive stress-strain data for PBX 9501. In addition Dienes (1998) was able to obtain a fit to the strain rate dependence of Wiegand's results only by introducing slow crack growth into his model. And modelers at AWE, Aldermaston have found a very low stress threshold for crack growth in EDC37. All of these results support the hypothesis that primarily slow crack growth and not rapid unstable crack growth occurs in compression in these composites for the conditions of interest here. The maximum stress observed in compression, the compressive strength, is then less than the stress required for rapid unstable crack growth and this latter stress is not observed for the reason given above. Returning then to equation (9) a calculation of the friction coefficient using the compressive strength and the tensile strength will yield a coefficient which is less than the true value because the compressive strength is less than the stress required for rapid unstable crack growth. Poisson's ratio has been found to be 0.42 for EDC37 in the low pressure range using neoprene shrouds and the system described above in the experimental section. The ratio of compressive to tensile strengths is 3.2 for the conditions of this work (Ellis, unpublished results). Then  $\mu$  obtained from equation (9) is 0.62 and this is listed in Table 3 as a lower limit. The agreement between two of the values of  $\mu$ , Table 2, as obtained from equations (6), and (8) and the minimum value as obtained from equation (9) provide significant support for the role of friction in determining the compressive stresses. Values of  $\mu$  for three other composite plastic bonded explosives obtained using equation (9) are somewhat close to the values for EDC37.

It is to be noted that at high strain rates the time available for slow crack growth for a given range of strain will be much less than the time needed for the same range of strains at low strain rates. Therefore, the damage introduced by slow crack growth will be less at the higher strain rate. Thus the sample will support larger stresses at the higher rate and so the stress may increase to that required for rapid unstable crack growth and fracture.

Because there is friction between crack surfaces associated with crack motion, there will be heating of the crack surfaces. This raises the possibility of ignition of reaction at crack surfaces because of this heating. Kuo and Dienes (2002) have presented evidence for reaction

at cracks surfaces taken from the work of Howe et al (Howe et al, 1985). These latter investigators impacted artillery shells containing TNT and afterwards polished TNT surfaces to reveal cracks. In particular, several cracks exhibited evidence of reaction along the crack length, thus giving support to the hypothesis of ignition due to frictional heating at the crack surfaces. In addition, Dienes et al (2006) have calculated particle velocity versus time curves which are very similar to the observed curves of Mulford et al, (1993) for PBX 9501 subjected to multiple shocks. Dienes et al used a model in which frictional heating in shear cracks raises the local temperature and pressure sufficiently to initiate reaction. Both of these works indicate the very practical importance of friction between the surfaces of cracks in explosives.

## 5. SUMMARY AND CONCLUSIONS

A linear increase of the compressive strength with increasing pressure is attributed to the effect of coulomb friction between the surfaces of closed shear cracks. The slope obtained from this linear relationship is proportional to the friction coefficient and is also dependent on the failure angle, the angle which the failure plane, the plane of maximum shear stress, makes with the loading direction. In addition, Dienes (1983) and Kuo and Dienes (2002) predict a relationship between the friction coefficient and only the failure angle. The friction coefficient obtained from the slope of the strength versus pressure curve and the failure angle is in substantial agreement with the coefficient obtained only from the failure angle. These authors also predict a relationship between the friction coefficient and the ratio of compressive strength to tensile strength, at atmospheric pressure. A lower limit on the value of the friction coefficient has been obtained from this relationship which is in agreement with the other values noted immediately above. This agreement of friction coefficients obtained from the three different relationships is taken as strong support for the role of friction in the mechanical properties of this composite.

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